

## Circles: Area and Circumference

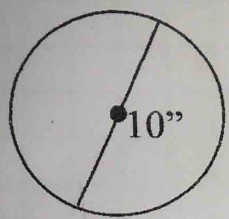
### Circumference

The circumference of a circle is the "perimeter" or distance around the circle.

\* LENGTH... one dimensional

Formulas:  $C = \pi d$  OR  $C = 2\pi r$

Example: Determine the circumference.



$$C = \pi d \quad (\text{Justify})$$

$$C = \pi \cdot 10 \quad (\text{plug in})$$

$$C = 10\pi \text{ inches} \quad (\text{exact answer})$$

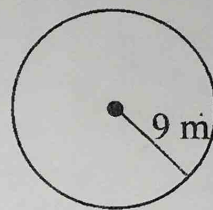
$$C \approx 31.42 \text{ inches} \quad (\text{approx answer})$$

### Area

The area of a circle is the region inside the circle.

Formula:  $A = \pi r^2$

\* TWO DIMENSIONAL measurement!!  
Example: Determine the area.



$$A = \pi r^2 \quad (\text{Justify})$$

$$A = \pi 9^2 \quad (\text{plug in})$$

$$A = 81\pi \text{ m}^2 \quad (\text{exact})$$

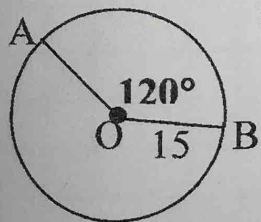
$$A \approx 254.47 \text{ m}^2 \quad (\text{approx})$$

### Arc Length

Length of an arc or distance from one end to the other (measured in ft, cm, in, etc... a portion of circumference)

Formulas: length of arc =  $\frac{\text{arc measure}}{360^\circ} \cdot \text{Circumference}$

Example: Determine the length of AB.



$$\text{length of } \overset{\text{arc measure}}{\text{portion}} \text{ AB} = \frac{120}{360} \cdot (2\pi \cdot 15)$$

$$= \frac{1}{3} (30\pi)$$

$$= 10\pi \text{ units}$$

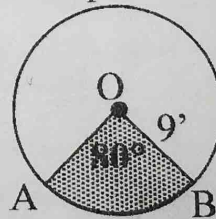
$$\approx 31.42 \text{ units}$$

### Area of a sector

The sector, or piece of a circle, formed by the two radii of a central angle and the arc between their endpoints on the circle. \* Portion of Area!

Formulas:  $A_{\text{sector}} = \frac{\text{arc measure}}{360^\circ} \cdot A_{\text{circle}}$

Example: Determine the area of sector AOB.



$$A_{\text{sector AOB}} = \frac{80}{360} \cdot (\pi 9^2)$$

$$= \frac{2}{9} (81\pi)$$

$$= 18\pi \text{ ft}^2$$

$$\approx 56.55 \text{ ft}^2$$