

Completing the Square

Given an expression in the form $ax^2 + bx + c$ where $a \neq 0$, this is the step-by-step process for completing the square to write the expression in vertex form.

<u>Description</u>	<u>Algebra</u>
1. Group variable terms away from the constant.	$ax^2 + bx + c$
2. Factor 'a' out of the two terms in the parentheses.	$(ax^2 + bx) + c$
3. Add $\left(\frac{1}{2} \cdot \frac{b}{a}\right)^2$ inside the parentheses, but this means keeping it the same by subtracting $a \cdot \left(\frac{b}{2a}\right)^2$ from the constant.	$a\left(x^2 + \frac{b}{a}x + \left(\frac{b}{2a}\right)^2\right) + c - a\left(\frac{b}{2a}\right)^2$
4. Rewrite the expression in vertex form.	$a\left(x + \frac{b}{2a}\right)^2 + \left(c - a\left(\frac{b}{2a}\right)^2\right)$

Example: Complete the square to write in vertex form.

$$A(x) = 3x^2 + 12x + 17$$

